**Instructions.** Write all answers clearly on one piece of paper, and put all group members' names on the top of the paper. If you talk, you must do so **very quietly**!

- 1. (True/False) Let  $n \in \mathbb{Z}$ , let G be a group, and let  $a \in G$ . If |G| divides n, then  $a^n = e$ .
- 2. Suppose that  $p \ge 3$  is a prime number. How many different groups are there of order 2p up to isomorphism?
- 3. How many permutations in  $S_4$  stabilize 1? This is the same as asking for the size of the set  $\{\phi \in S_4 | \phi(1) = 1\}$ .
- 4. The orbit of an element s in a group G is defined as  $\operatorname{orb}_G(s) = \{\phi(s) \mid \phi \in G\}$ . What is  $\operatorname{orb}_G(4)$  when  $G = \langle (135)(246) \rangle$ ?